

# COMP331/557: Optimisation

## Introduction to Gurobi

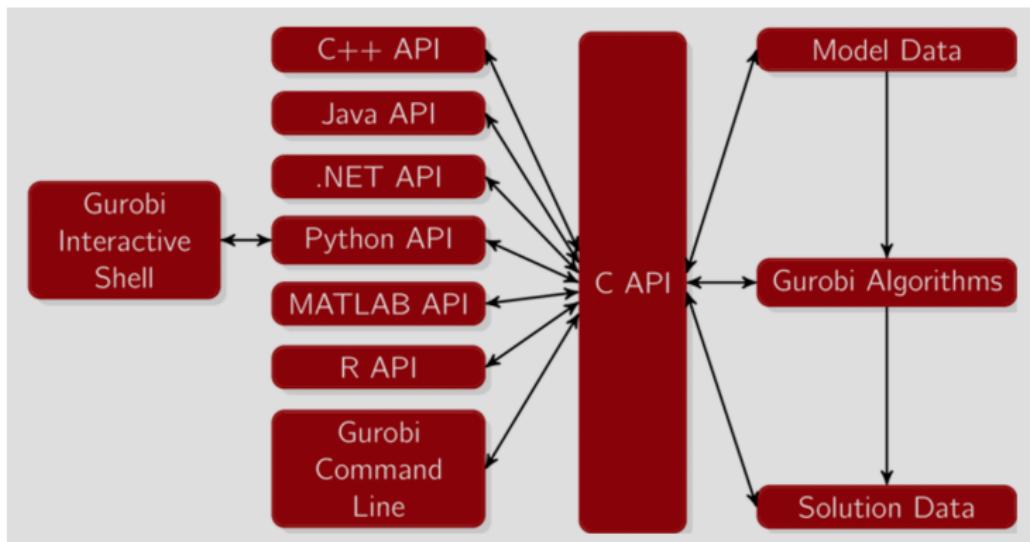
# Outline

- ① Gurobi
- ② Gurobi Python Interface
- ③ Solving a model in Gurobi
- ④ Building a Model from Scratch
- ⑤ Solving a Model in a Python script

## What is Gurobi?

- ▶ State-of-the-art simplex based linear programming (LP) and mixed-integer programming (MIP) solver.
- ▶ Built from the ground up to exploit modern multi-core processors.
- ▶ Developed by
  - ▶ Zonghao Gu
  - ▶ Edward Rothberg
  - ▶ Robert Bixby
- (the brains behind CPLEX)
- ▶ Performance is comparable to CPLEX.
- ▶ Many resources available from the Gurobi website ([www.gurobi.com](http://www.gurobi.com))
  - ▶ Videos, Code Examples, ...
  - ▶ Reference Manual (in particular Section 6)  
<http://www.gurobi.com/documentation/8.0/refman.pdf>

# Gurobi Language Interfaces



Picture taken from <http://www.gurobi.com>

- ▶ We will use the **Gurobi Interactive Shell**,
  - ▶ i.e., a **Python shell** with Gurobi modules pre-imported

## Python: What is it?

- ▶ Object oriented scripting language.
- ▶ Interpreted rather than being compiled.
- ▶ Easy to learn, read, use.
- ▶ Code is usually shorter and more readable.
- ▶ Open source
- ▶ `python.org`: "*Python is a programming language that lets you work quickly and integrate systems more effectively.*"
  
- ▶ We will not need much Python.
- ▶ If you want to learn more, I recommend this:  
<http://heather.cs.ucdavis.edu/~matloff/Python/PLN/FastLanePython.pdf>

## Some Python Examples: Lists

```
>>> x = [5,10,16,300]
```

```
>>> x
```

```
[5, 10, 16, 300]
```

```
>>> x.append(-3)
```

```
>>> x
```

```
[5, 10, 16, 300, -3]
```

```
>>> del x[1]
```

```
>>> x
```

```
[5, 16, 300, -3]
```

```
>>> y=x[2:]
```

```
>>> y
```

```
[300, -3]
```

```
>>> x.insert(2,49)
```

```
>>> x
```

```
[5, 16, 49, 300, -3]
```

## Some Python Examples: Lists

```
>>> x = [5,10,16,300]
>>> x
[5, 10, 16, 300]
```

```
>>> x.append(-3)
>>> x
[5, 10, 16, 300, -3]
```

```
>>> del x[1]
>>> x
[5, 16, 300, -3]
```

```
>>> y=x[2:]
>>> y
[300, -3]
```

```
>>> x.insert(2,49)
>>> x
[5, 16, 49, 300, -3]
```

```
>>> x.remove(300)
>>> x
[5, 16, 49, -3]
```

```
>>> x.index(16)
1
```

```
>>> y=['python','gurobi']
>>> y
['python', 'gurobi']
```

```
>>> z=x+y
>>> z
[5, 16, 49, -3, 'python', 'gurobi']
```

```
>>> z=2*x
>>> z
[5, 16, 49, -3, 5, 16, 49, -3]
```

## Some Python Examples: Lists

```
>>> x = [5,10,16,300]
>>> x
[5, 10, 16, 300]

>>> x.append(-3)
>>> x
[5, 10, 16, 300, -3]

>>> del x[1]
>>> x
[5, 16, 300, -3]

>>> y=x[2:]
>>> y
[300, -3]

>>> x.insert(2,49)
>>> x
[5, 16, 49, 300, -3]

>>> x.remove(300)
>>> x
[5, 16, 49, -3]

>>> x.index(16)
1

>>> y=['python','gurobi']
>>> y
['python', 'gurobi']

>>> z=x+y
>>> z
[5, 16, 49, -3, 'python', 'gurobi']

>>> z=2*x
>>> z
[5, 16, 49, -3, 5, 16, 49, -3]
```

In most other programming languages you need much more code to do this.

# Solving a Model in Gurobi

lp1.lp

```
Minimize
  2 x + 4 y
Subject To
  R0: x + y >= 3
  R1: 3 x + 2 y >= 14
  R2: 3 x + 2 y <= 14
Bounds
  x <= 10
  y >= 1
End
```

- ▶ Start Gurobi by typing `gurobi` in terminal
- ▶ Read model file `lp1.lp`  
`m=read('lp1.lp')`
- ▶ Optimize model  
`m.optimize()`
- ▶ Print solution  
`m.getVars()`
- ▶ Write solution to file:  
`m.write('lp1.sol')`
- ▶ System call to output `lp1.sol` file:  
`system('cat lp1.sol')`

Short documentation on the supported LP-file format:

[http://www.gurobi.com/documentation/8.0/refman/lp\\_format.html](http://www.gurobi.com/documentation/8.0/refman/lp_format.html)

# Building a Model from Scratch

## Brewery Example

$$\begin{aligned} \text{max } & 13A + 23B \\ \text{s.t. } & 5A + 15B \leq 480 \\ & 4A + 4B \leq 160 \\ & 35A + 20B \leq 1190 \\ & A, B \geq 0 \\ & A, B \text{ integer} \end{aligned}$$

- ▶ Call the model constructor  
`m=Model('brewery')`
- ▶ Add variables  
`A=m.addVar(vtype=GRB.INTEGER, name="Ale")`  
`B=m.addVar(vtype=GRB.INTEGER, name="Beer")`  
`m.update()`
- ▶ Add objective function and constraints  
`m.setObjective(13*A + 23*B, GRB.MAXIMIZE)`  
`c1=m.addConstr(5*A + 15*B <= 480)`  
`c2=m.addConstr(4*A + 4*B <= 160)`  
`c3=m.addConstr(35*A + 20*B <= 1190)`
- ▶ Optimize and Output Solution  
`m.optimize()`  
`m.getVars()`

# Solving a Model in a Python script

brewery.py

```
# import gurobi libraries
from gurobipy import *

m=Model('brewery')

# Add Variables
A=m.addVar(vtype=GRB.INTEGER, name="Ale")
B=m.addVar(vtype=GRB.INTEGER, name="Beer")
m.update()

# Add Constraints
c1=m.addConstr(4*A + 4*B <= 160)
c2=m.addConstr(35*A + 20*B <= 1190)
c3=m.addConstr(5*A + 15*B <= 480)

# Add Objective Function
m.setObjective(13*A + 23*B, GRB.MAXIMIZE)

# Optimize Model
m.optimize()

# Output formatted solution
for v in m.getVars():
    print v.varName, v.x
print 'Obj:', m.objVal
```

► Run this by calling

python brewery.py  
from the shell