## Tutorials

## Optimisation <br> 2018

## Exercise Sheet 5

## Exercise 8:

Consider the following linear program:

$$
\begin{aligned}
& \min -\frac{3}{4} x_{1}+20 x_{2}-\frac{1}{2} x_{3}+6 x_{4}-3 \\
& \text { s.t. } \quad \frac{1}{4} x_{1}-8 x_{2}-x_{3}+9 x_{4} \leq 0 \\
& \frac{1}{2} x_{1}-12 x_{2}-\frac{1}{2} x_{3}+3 x_{4} \leq 0 \\
& x_{3} \quad \leq 1 \\
& x_{1}, \quad x_{2}, \quad x_{3}, \quad x_{4} \geq 0
\end{aligned}
$$

Use the Simplex method (following the Bland's rule) in order to find the optimal objective function. Hint: This is the example from the lectures which is cycling.
(a) You should first figure out from which iteration on things will be different.
(b) Do only the final iterations.

## Exercise 9:

While solving a standard form problem, we arrive at the following tableau, with $x_{3}, x_{4}$, and $x_{5}$ being the basic variables:

$x_{3}=$|  | $x_{1}$ | $x_{2}$ | $x_{3}$ | $x_{4}$ | $x_{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -10 | $\delta$ | -2 | 0 | 0 | 0 |
| $x_{4}=$4 -1 $\eta$ 1 0 0 <br> 1 $\alpha$ -4 0 1 0 <br> $x_{5}$ $\gamma$ 3 0 0 1 l |  |  |  |  |  |

The entries $\alpha, \beta, \gamma, \delta, \eta$ in the tableau are unknown parameters. For each of the following statements, find some parameter values that will make the statement true:
(a) The current solution is infeasible.
(b) The current solution is feasible but not optimal.
(c) The optimal cost is $-\infty$.
(d) The current solution is optimal and there are multiple optimal solutions.

## Exercise 10:

Consider the following linear program:

$$
\begin{array}{rrl}
\min & 4 x_{1}+4 x_{2}+x_{3} \\
\text { s.t. } & x_{1}+x_{2}+x_{3} & =2 \\
& 2 x_{1}+x_{2} & =3 \\
& 3 x_{1}+2 x_{2}+x_{3} & =5 \\
& x_{1}, x_{2}, x_{3} & \geq 0
\end{array}
$$

Solve this LP with the Simplex Method using the Big-M method.

